# Learning Representations of Bi-Level Knowledge Graphs for Reasoning beyond Link Prediction

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## **Knowledge Graphs**

- Knowledge Graphs represent known facts using triplets.
  - Knowledge Graph Embedding represents entities and relations as feature vectors.





## **Relationships between Triplets**

- Each triplet can have a relationship with another triplet.
  - *T*<sub>1</sub>: (Joe Biden, HoldsPosition, Vice President)
  - *T*<sub>2</sub>: (Barack Obama, HoldsPosition, President)
- Higher-Level Triplets represent the relationships between triplets.
  - $\langle T_1, \text{WorksFor}, T_2 \rangle$ 
    - Joe Biden was a vice president when Barack Obama was a president.
  - Connects triplets using the Higher-Level Relations.



## **Bi-Level Knowledge Graphs**

- Base-level Triplets
  - Relationships between entities
- Higher-level Triplets
  - Relationships between base-level triplets



**Base-Level Triplets** 



## **Reasoning beyond Link Prediction**

### Triplet Prediction

- Predicts a triplet that is likely to be connected to a given triplet.
- (Beckham, HasNationality, England), PrerequisiteFor, ?)
  - Answer: (Beckham, PlaysFor, England National Football Team)





## **Reasoning beyond Link Prediction**

### Conditional Link Prediction

- Predicts a missing entity in a triplet where another triplet is provided as a condition.
- ((Joe Biden, HoldsPosition, Vice President), WorksFor, (?, HoldsPosition, President))
  - Answer: Barack Obama





## Contributions

- Define **Bi-Level Knowledge Graphs** and create three real-world datasets
- Propose an efficient data augmentation strategy on a bi-level KG
- Develop **BiVE** (embedding of **Bi**-le**V**el knowledg**E** graphs)
- Two new tasks: Triplet Prediction and Conditional Link Prediction
  - BiVE outperforms 12 different state-of-the-art methods.



## **Bi-Level Knowledge Graphs**

- A base-level knowledge graph  $G = (\mathcal{V}, \mathcal{R}, \mathcal{E})$ 
  - $\mathcal{V}$ : Set of entities,  $\mathcal{R}$ : Set of relations,  $\mathcal{E}$ : Set of triplets
- A set of Higher-Level Triplets  $\mathcal{H} = \{\langle T_i, \hat{r}, T_j \rangle : T_i \in \mathcal{E}, \hat{r} \in \hat{\mathcal{R}}, T_j \in \mathcal{E}\}$ 
  - $\hat{\mathcal{R}}$ : Set of Higher-Level Relations
- A Bi-Level Knowledge Graph  $\hat{G} = (\mathcal{V}, \mathcal{R}, \mathcal{E}, \hat{\mathcal{R}}, \mathcal{H})$ 
  - Add higher-level triplets to the base-level KG by introducing the higher-level relations



## **Real-World Bi-Level KGs**

- Create three real-world bi-level knowledge graphs: FBH, FBHE, DBHE
  - *FBH* and *FBHE* are based on *FB15K237* from *Freebase*.
  - *DBHE* is based on *DB15K* from *DBpedia*.
- Add the higher-level triplets to the base-level knowledge graphs
  - FBHE and DBHE contain some externally-sourced knowledge.
- Number of higher-level relations in the datasets
  - FBH: 6, FBHE: 10, DBHE: 8



## **Real-World Bi-Level KGs**

	<b>Higher-Level Relation</b>	Higher-Level Triplet				
	ŕ	$\langle T_i, \hat{r}, T_j \rangle$				
	DroroquioitoFor	$T_i$ : (BAFTA Award, Nominates, The King's Speech)				
FBHE	Prerequisiteror	$T_j$ : (The King's Speech, Wins, BAFTA Award)				
	ImpliesDrefession	$T_i$ : (Liam Neeson, ActsIn, Love Actually)				
	ImpliesProtession	$T_j$ : (Liam Neeson, IsA, Actor)				
	WarkoFor	$T_i$ : (Joe Biden, HoldsPosition, Vice President)				
	VVOIKSFOI	<i>T<sub>j</sub></i> : (Barack Obama, HoldsPosition, President)				
	SucceededBy	$T_i$ : (George W. Bush, HoldsPosition, President)				
	Succeededby	<i>T<sub>j</sub></i> : (Barack Obama, HoldsPosition, President)				
	ImpliesTimeZone	$T_i$ : (Czech Republic, TimeZone, Central European)				
DBHE	implies i mezone	$T_j$ : (Prague, TimeZone, Central European)				
	NovtAlmoMotor	$T_i$ : (Gerald Ford, StudiesIn, University of Michigan)				
	NextAimaiviatei	<i>T<sub>j</sub></i> : (Gerald Ford, StudiesIn, Yale University)				



## Data Augmentation on a Bi-Level KG

- Propose a Data Augmentation Strategy based on Random Walks
- Randomly visit a neighbor by following a base-level or a higher-level triplet.
  - Do not allow going back to an entity that has already been visited.
- Random Walk Path
  - Sequence of visited entities, relations and higher-level relations



Random walk path: 
$$(h_0, r_0, h_i, r_i, \hat{r}, r_j, t_j)$$



## **Relation Sequence**

- Relation Sequence  $(p_k)$ 
  - Sequence of relations and higher-level relations extracted from a random walk path.



- Confidence Score  $c(p_k, r)$ 
  - Probability that the entity pair connected by  $p_k$  is also connected by r.
- Add the missing plausible triplets based on the confidence score.



## **Example: Augmented Triplets**



r: Plays







- Loss incurred by the base-level triplets
  - $L_{\text{base}} = \sum_{(h,r,t)\in\mathcal{E}_{\text{train}}} g(-f(\mathbf{h},\mathbf{r},\mathbf{t})) + \sum_{(h',r',t')\in\mathcal{E}'_{\text{train}}} g(f(\mathbf{h}',\mathbf{r}',\mathbf{t}'))$ 
    - $g(x) = \log(1 + \exp(x))$
    - $\mathcal{E}'_{train}$  is a set of corrupted triplets.
    - We can use any knowledge graph embedding scoring function for  $f(\cdot)$ .
- We implement BiVE with two different scoring functions.
  - **BiVE-Q**: Uses scoring function of QuatE \*
  - **BiVE-B**: Uses scoring function of BiQUE \*\*

\* QuatE: Zhang et al., Quaternion Knowledge Graph Embeddings, NeurIPS 2019 \*\* BiQUE: Guo et al., BiQUE: Biquaternionic Embeddings of Knowledge Graphs, EMNLP 2021

Beckham

England

Has

**Nationality** 



Beckham

England

Nationa

Footbal Team

**Plays** 

For

- Given  $T_i = (h_i, r_i, t_i)$ , let  $\mathbf{T}_i$  denote an embedding vector of  $T_i$ .
  - Define  $\mathbf{T}_i = \boldsymbol{W}[\mathbf{h}_i; \mathbf{r}_i; \mathbf{t}_i]$ 
    - W is a projection matrix.
- Loss incurred by the higher-level triplets

• 
$$L_{\text{high}} = \sum_{(T_i, \hat{r}, T_j) \in \mathcal{H}_{\text{train}}} g\left(-f(\mathbf{T}_i, \hat{\mathbf{r}}, \mathbf{T}_j)\right) + \sum_{(T'_i, \hat{r}', T'_j) \in \mathcal{H}'_{\text{train}}} g\left(f(\mathbf{T}'_i, \hat{\mathbf{r}}', \mathbf{T}'_j)\right)$$

•  $\mathcal{H}'_{train}$  is a set of corrupted higher-level triplets.

Beckham,

HasNationality, England

Beckham.

PlaysFor, England National Football Team

PrerequisiteFor

- Loss incurred by the augmented triplets
  - $L_{\text{aug}} = \sum_{(h,r,t)\in\mathcal{S}} g(-f(\mathbf{h},\mathbf{r},\mathbf{t})) + \sum_{(h',r',t')\in\mathcal{S}'} g(f(\mathbf{h}',\mathbf{r}',\mathbf{t}'))$ 
    - S is a set of augmented triplets.
    - $\mathcal{S}'$  is a set of corrupted triplets.
- Loss function of BiVE
  - $L_{\text{BiVE}} = L_{\text{base}} + \lambda_1 \cdot L_{\text{high}} + \lambda_2 \cdot L_{\text{aug}}$ 
    - $\lambda_1$  and  $\lambda_2$  control the importance of  $L_{high}$  and  $L_{aug}$ , respectively.





## **Scoring Functions of BiVE**

### Triplet Prediction

- Given an incomplete higher-level triplet  $\langle T_i, \hat{r}, ? \rangle$ ,
  - BiVE computes  $F_{tp}(X) = f(\mathbf{T}_i, \hat{\mathbf{r}}, \mathbf{X})$  for every base-level triplet  $X \in \mathcal{E}_{train}$ .
  - Rank base-level triplets based on the calculated scores.

### Conditional Link Prediction

- Given an incomplete higher-level triplet  $\langle T_i, \hat{r}, (h_j, r_j, ?) \rangle$ ,
  - BiVE compute  $F_{clp}(x) = f(\mathbf{h}_j, \mathbf{r}_j, \mathbf{x}) + \lambda_1 \cdot f(\mathbf{T}_i, \hat{\mathbf{r}}, W[\mathbf{h}_j; \mathbf{r}_j; \mathbf{x}])$  for every entity  $\mathbf{x} \in \mathcal{V}$ .
  - Rank entities based on the calculated scores.



## **Experimental Settings**

#### Datasets

- Three real-world bi-level KGs: FBH, FBHE, DBHE
- Split  $\mathcal{E}$  and  $\mathcal{H}$  into training, validation, test sets with a ratio of 8:1:1.

	$ \mathcal{V} $	$ \mathcal{R} $	<i>8</i>	$\left \widehat{\mathcal{R}} ight $	$ \mathcal{H} $	$ \hat{\mathcal{E}} $
FBH	14,541	237	310,117	6	27,062	33,157
FBHE	14,541	237	310,117	10	34,941	33,719
DBHE	12,440	87	68,296	8	6,717	8,206

 $|\hat{\mathcal{E}}|$  is the number of base-level triplets involved in the higher-level triplets



## **Experimental Settings**

- Baselines: 12 different state-of-the-art methods
  - String matching: ASER
  - Path finding: MINERVA, Multi-Hop
  - Rule or logic: AnyBURL, Neural-LP, DRUM
  - Relation path: PTransE, RPJE
  - Latent space: TransD, ANALOGY, QuatE, BiQUE
- We repeat experiments ten times for each method.



## **Results of Triplet Prediction**

		FBH			FBHE			DBHE		
	MR(↓)	MRR(↑)	Hit@10(↑)	$MR(\downarrow)$	MRR(↑)	Hit@10(↑)	$MR(\downarrow)$	MRR(↑)	Hit@10(↑)	
ASER	74541.7	0.011	0.015	57916.0	0.050	0.070	18157.6	0.042	0.075	
MINERVA	109055.1	0.093	0.113	85571.5	0.220	0.300	20764.3	0.177	0.221	
Multi-Hop	108731.7	0.105	0.117	83643.8	0.255	0.311	20505.8	0.191	0.230	
Neural-LP	115016.6	0.070	0.073	90000.4	0.238	0.274	21130.5	0.170	0.209	
DRUM	115016.6	0.069	0.073	90000.3	0.261	0.274	21130.5	0.166	0.209	
AnyBURL	108079.6	0.096	0.108	83136.8	0.191	0.252	20530.8	0.177	0.214	
PTransE	111024.3	0.069	0.071	86793.2	0.249	0.274	18888.7	0.158	0.195	
RPJE	113082.0	0.070	0.072	89173.1	0.267	0.274	20290.4	0.166	0.206	
TransD	74277.3	0.052	0.104	52159.4	0.238	0.280	16698.1	0.116	0.189	
ANALOGY	93383.4	0.072	0.107	60161.5	0.286	0.318	18880.0	0.150	0.211	
QuatE	145603.8	0.103	0.114	94684.4	0.101	0.209	26485.0	0.157	0.179	
BiQUE	81687.5	0.104	0.115	61015.2	0.135	0.205	19079.4	0.163	0.185	
BiVE-Q	18.7	0.748	0.853	33.1	0.531	0.683	56.6	0.315	0.523	
BiVE-B	19.7	0.731	0.837	27.9	0.555	0.718	4.7	0.644	0.914	



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## **Results of Conditional Link Prediction**

		FBH			FBHE			DBHE	
	MR(↓)	MRR(↑)	Hit@10(↑)	MR(↓)	MRR(↑)	Hit@10(↑)	MR(↓)	MRR(↑)	Hit@10(↑)
ASER	1183.9	0.251	0.316	970.7	0.289	0.382	1893.5	0.225	0.348
MINERVA	3817.8	0.328	0.415	3018.5	0.407	0.492	2934.1	0.362	0.433
Multi-Hop	1878.2	0.421	0.578	1447.3	0.443	0.615	1012.3	0.442	0.652
Neural-LP	185.9	0.433	0.648	146.2	0.466	0.716	32.2	0.517	0.756
DRUM	262.7	0.394	0.555	207.6	0.413	0.620	49.0	0.470	0.732
AnyBURL	228.5	0.380	0.563	166.0	0.418	0.607	81.7	0.403	0.594
PTransE	214.8	0.440	0.686	167.0	0.516	0.752	19.3	0.505	0.780
RPJE	212.5	0.440	0.686	159.0	0.528	0.753	19.3	0.504	0.779
TransD	190.1	0.300	0.496	165.6	0.363	0.529	35.5	0.436	0.708
ANALOGY	341.0	0.182	0.291	113.3	0.409	0.581	279.1	0.140	0.253
QuatE	163.7	0.346	0.494	1546.4	0.124	0.189	551.6	0.208	0.309
BiQUE	111.0	0.423	0.641	90.1	0.387	0.617	29.5	0.378	0.677
BiVE-Q	7.0	0.752	0.906	11.0	0.698	0.839	12.5	0.606	0.828
BiVE-B	6.6	0.762	0.911	12.8	0.696	0.834	3.2	0.801	0.958



## **Example: Conditional Link Prediction**

- Example 1
  - ((Joe Jonas, IsA, ?), ImpliesProfession, (Joe Jonas, IsA, Actor))
    - Answer: Voice Actor
  - ((Joe Jonas, IsA, ?), ImpliesProfession, (Joe Jonas, IsA, Musician))
    - Answer: Singer-songwriter
- Example 2
  - (Saturn Award, Nominates, Avatar), PrerequisiteFor, (Avatar, Wins, ?))
    - Answer: Saturn Award
  - ((Academy Awards, Nominates, Avatar), PrerequisiteFor, (Avatar, Wins, ?))
    - Answer: Academy Awards



## **Results of Base-Level Link Prediction**

• Our BiVE models show comparable results to the baseline methods.

 BiVE models have the extra capability of dealing with the Triplet Prediction and Conditional Link Prediction tasks.

FBH FBHE DBHE
Hit@10(↑) Hit@10(↑) Hit@10(↑)
ASER 0.323 0.323 0.197
MINERVA 0.339 0.339 0.297
Multi-Hop 0.500 0.500 0.404
Neural-LP 0.486 0.486 0.357
DRUM 0.490 0.490 0.359
AnyBURL 0.526 0.526 0.364
PTransE 0.333 0.333 0.277
RPJE 0.368 0.368 0.341
TransD 0.527 0.527 0.423
ANALOGY 0.486 0.486 0.323
QuatE 0.581 0.581 0.440
BiQUE 0.583 0.583 0.446
BiVE-Q 0.584 0.584 0.438
BiVE-B 0.586 0.586 0.444



## **Example: Augmented Triplets**

• Our augmented triplets include many ground-truth triplets that were missing in the training set.

Relation Sequence $p_k$	Relation r	$c(p_k,r)$	Examples of the Augmented Triplets
Plays, Plays <sup>-1</sup> , ImpliesSports, HasPosition	HasPosition	0.78	(Bayer 04 Leverkusen, HasPosition, Forward)
IsPartOf, IsPartOf, ImpliesLocation, IsPartOf	IsPartOf	0.76	(San Pedro, IsPartOf, California)

 $c(p_k, r)$  is the confidence score of the pair  $(p_k, r)$ 

	FBH	FBHE	DBHE
No. of augmented triplets	16,601	17,463	2,026
$ S \cap \mathcal{E}_{valid}  +  S \cap \mathcal{E}_{test} $	5,237	5,380	316

No. of augmented triplets contained in either  $\mathcal{E}_{valid}$  or  $\mathcal{E}_{test}$ 



## Conclusion

- Define a Bi-Level Knowledge Graph
- Propose a Random-Walk based Data Augmentation Strategy on bi-level KGs
- BiVE takes into account the structures of the base-level triplets, the higher-level triplets and the augmented triplets.
- BiVE significantly outperforms state-of-the-art methods in terms of the two newly defined tasks: Triplet Prediction and Conditional Link Prediction
- Our method can contribute to advancing many knowledge-based applications, including Conditional QA and Multi-Hop QA.



## Thanks!

Our datasets and codes are available at:

https://github.com/bdi-lab/BiVE

You can find us at:

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### **Differences between BiVE and Rule-based Methods**

### Rule-based Methods

- Only consider the relationships between entities
- Consider the first-order-logic-like rules between connected entities
  - e.g.,  $\forall x, y, z: (x, r_1, y) \land (y, r_2, z) \Rightarrow (x, r_3, z)$

### • BiVE

- Considers the relationships between entities and the relationships between triplets
- Entities are **not necessarily connected** by the base-level triplets, and the patterns are **not restricted to the first-order-logic-like formula**

• e.g., 
$$(x, r_1, y) \stackrel{\hat{r}}{\Rightarrow} (p, r_2, q)$$

